

TABLA DE DERIVADAS ELEMENTALES

FUNCIONES SIMPLES		FUNCIONES COMPUESTAS (Regla de la cadena)	
$y=k$	$y'=0$		
$y=x$	$y'=1$		
$y=k \cdot x$	$y'=k$	$y=k \cdot u$	$y'=k \cdot u'$
$y=x^n \ (n \in \mathfrak{R})$	$y'=n \cdot x^{n-1}$	$y=u^n \ (n \in \mathfrak{R})$	$y'=n \cdot u^{n-1} \cdot u'$
		$y=u \pm v$	$y'=u' \pm v'$
		$y=u \cdot v$	$y'=u' \cdot v + u \cdot v'$
		$y = \frac{u}{v}$	$y' = \frac{u' \cdot v - u \cdot v'}{v^2}$
$y = \frac{1}{x}$	$y = -\frac{1}{x^2}$	$y = \frac{1}{u}$	$y = -\frac{u'}{u^2}$
$y = \sqrt{x}$	$y = \frac{1}{2\sqrt{x}}$	$y = \sqrt{u}$	$y = \frac{u'}{2\sqrt{u}}$
$y = \sqrt[n]{x}$	derivarla como $y=x^{1/n}$	$y = \sqrt[n]{u}$	derivarla como $y=u^{1/n}$
$y=a^x$	$y'=a^x \cdot \ln a$	$y=a^u$	$y'=u' \cdot a^u \cdot \ln a$
$y=e^x$	$y'=e^x$	$y=e^u$	$y'=e^u \cdot u'$
		$y=u^v$	aplicar derivación logarítmica
$y=\log_a x$	$y' = \frac{\log_a e}{x} = \frac{1}{x \cdot \ln a}$	$y=\log_a u$	$y' = \frac{u' \cdot \log_a e}{u} = \frac{u'}{u \cdot \ln a}$
$y=\ln x$	$y' = \frac{1}{x}$	$y=\ln u$	$y' = \frac{u'}{u}$
$y=\text{sen } x$	$y'=\text{cos } x$	$y=\text{sen } u$	$y'=u' \cdot \text{cos } u$
$y=\text{cos } x$	$y'=-\text{sen } x$	$y=\text{cos } u$	$y'=-u' \cdot \text{sen } u$
$y=\text{tg } x$	$y' = 1 + \text{tg}^2 x = \frac{1}{\text{cos}^2 x}$	$y=\text{tg } u$	$y' = (1 + \text{tg}^2 u) \cdot u' = \frac{u'}{\text{cos}^2 u}$
$y=\text{ctg } x$	$y' = -(1 + \text{ctg}^2 x) = \frac{-1}{\text{sen}^2 x}$	$y=\text{ctg } u$	$y' = -(1 + \text{ctg}^2 u) \cdot u' = \frac{-u'}{\text{sen}^2 u}$
$y=\text{arc sen } x$	$y' = \frac{1}{\sqrt{1-x^2}}$	$y=\text{arc sen } u$	$y' = \frac{u'}{\sqrt{1-u^2}}$
$y=\text{arc cos } x$	$y' = \frac{-1}{\sqrt{1-x^2}}$	$y=\text{arc cos } u$	$y' = \frac{-u'}{\sqrt{1-u^2}}$
$y=\text{arc tg } x$	$y' = \frac{1}{1+x^2}$	$y=\text{arc tg } u$	$y' = \frac{u'}{1+u^2}$
$y=\text{arc ctg } x$	$y' = \frac{-1}{1+x^2}$	$y=\text{arc ctg } u$	$y' = \frac{-u'}{1+u^2}$

En esta tabla, k y n son números reales, a es un número real positivo, y u y v son funciones.